Converting from one unit to another

We will use the method of dimensional analysis, sometimes called the factor-label method.
... or, the "drag and drop" method!

Dimensional analysis uses conversion factors to change between one unit and another

What's a conversion factor? A simple equality.

Example

$$\boxed{12\ \text{in} = 1\ \text{ft}}$$

Conversion factors in metric

In the metric system, conversion factors between units may always be made from the metric prefixes!

For example, "kilo-" means 10^3

$$k = 10^3$$

so

$$kg = 10^3 g$$

$$km = 10^3 m$$

$$ks = 10^3 s$$

$$kL = 10^3 L$$

Just apply the prefix to the base unit!

How do we actually USE a conversion factor?

Convert 15.75 m to cm

$cm = 10^{-2} m$

$15.75\,\cancel{m} \times \dfrac{cm}{10^{-2}\,\cancel{m}} = \boxed{1575\ cm}$

* This fraction equals one, so multiplying by it does not change the VALUE of the number, only its UNITS!

* Similar to...

If X = 2, then

$\dfrac{X}{2} = 1$

15.75 / $\boxed{EE}$ −2 .. on TI-83

Convert 0.01893 kg to g

$Kg = 10^{3} g$

$0.01893\,\cancel{kg} \times \dfrac{10^{3}\,g}{\cancel{Kg}} = \boxed{18.93\ g}$

DRAG AND DROP

- Drag the part of the factor that contains the unit you want to get rid of (cancel out) to the BOTTOM.

- Then, drag the other half of the factor to the TOP

Convert 14500 mg to kg

$mg = 10^{-3} g$ $kg = 10^{3} g$

$$14500\, \cancel{mg} \times \frac{10^{-3}\, \cancel{g}}{\cancel{mg}} \times \frac{kg}{10^{3}\, \cancel{g}} = \boxed{0.0145\, kg}$$

Convert 0.147 cm^2 to m^2

$cm = 10^{-2} m$

$$0.147\, \cancel{cm^2} \times \frac{10^{-2}\, m}{\cancel{cm}} \times \frac{10^{-2}\, m}{\cancel{cm}} = \boxed{1.47 \times 10^{-5}\, m^2}$$

$0.000147\, m^2$

When converting squared or cubed units, use each factor two (for squared) or three (for cubed) times.

$cm^2 = cm \times cm$ $cm^3 = cm \times cm \times cm$

8.45 kg to μg

$Kg = 10^3 g$ $\mu g = 10^{-6} g$

$$8.45\ \cancel{Kg} \times \frac{10^3\ \cancel{g}}{\cancel{K}g} \times \frac{\mu g}{10^{-6}\ \cancel{g}} = \boxed{8450000000\ \mu g}$$

$8.45 \times 10^9\ \mu g$

88100 kHz to MHz $KHz = 10^3 Hz$

$\boxed{Hz = s^{-1}\ (\text{Frequency})}$

$MHz = 10^6 Hz$

$$88100\ K\cancel{Hz} \times \frac{10^3\ \cancel{Hz}}{K\cancel{Hz}} \times \frac{MHz}{10^6\ \cancel{Hz}} = \boxed{88.1\ MHz}$$

Convert 38.47 in to m, assuming 2.54 cm = 1 in

$2.54\,cm = in \qquad cm = 10^{-2}\,m$

$$38.47\,\cancel{in} \times \frac{2.54\,\cancel{cm}}{\cancel{in}} \times \frac{10^{-2}\,m}{\cancel{cm}} = \boxed{0.9771\,m}$$

Convert 12.48 km to in

$2.54\,cm = in \qquad cm = 10^{-2}\,m \qquad km = 10^{3}\,m$

$$12.48\,\cancel{km} \times \frac{10^{3}\,\cancel{m}}{\cancel{km}} \times \frac{\cancel{cm}}{10^{-2}\,\cancel{m}} \times \frac{in}{2.54\,\cancel{cm}} = \boxed{491300\,in}$$