

A balloon is taken from a room where the temperature is 27.0 C to a freezer where the temperature is -5.0 C. If the balloon has a volume of 3.5 L in the 27.0 C room, what is the volume of the balloon in the freezer. Assume pressure is constant.

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \text{ but } P_1 = P_2 ; \quad \frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$\frac{(3.5 \text{ L})}{(300.2 \text{ K})} = \frac{V_2}{(268.2 \text{ K})}$$

$$\boxed{3.1 \text{ L}} = V_2$$

$$V_1 = 3.5 \text{ L}$$

$$T_1 = 27.0^\circ\text{C} = 300.2 \text{ K}$$

$$V_2 = ?$$

$$T_2 = -5.0^\circ\text{C} = 268.2 \text{ K}$$

2.25 L of nitrogen gas is trapped in a piston at 25.0 C and 1.00 atm pressure. If the piston is pushed in so that the gas's volume is 1.00 L while the temperature increases to 31.0 C, what is the pressure of the gas in the piston?

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{(1.00 \text{ atm})(2.25 \text{ L})}{(298.2 \text{ K})} = \frac{P_2 (1.00 \text{ L})}{(304.2 \text{ K})}$$

$$\boxed{2.30 \text{ atm}} = P_2$$

$$P_1 = 1.00 \text{ atm}$$

$$V_1 = 2.25 \text{ L}$$

$$T_1 = 25.0^\circ\text{C} = 298.2 \text{ K}$$

$$P_2 = ?$$

$$V_2 = 1.00 \text{ L}$$

$$T_2 = 31.0^\circ\text{C} = 304.2 \text{ K}$$

Calculate the mass of ^{*}22650 L of oxygen gas at 25.0 C and 1.18 atm pressure.



*Volume of a 10'x10'x8' room

1 - Use the IDEAL GAS EQUATION ($PV=nRT$) to find MOLES of oxygen gas.

2 - Convert the moles of oxygen gas to mass using FORMULA WEIGHT.

$$PV = nRT \quad \left| \quad P = 1.18 \text{ atm} \quad R = 0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}} \right.$$

$$n = \frac{PV}{RT} \quad \left| \quad V = 22650 \text{ L} \quad T = 25.0^\circ\text{C} = 298.2 \text{ K} \right.$$

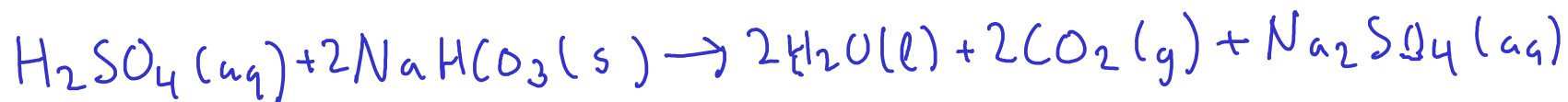
$$\textcircled{1} n_{\text{O}_2} = \frac{(1.18 \text{ atm})(22650 \text{ L})}{\left(0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}}\right)(298.2 \text{ K})} = 1092.222357 \text{ mol O}_2$$

$$\textcircled{2} 32.00 \text{ g O}_2 = \text{mol O}_2$$

$$1092.222357 \text{ mol O}_2 \times \frac{32.00 \text{ g O}_2}{\text{mol O}_2} = \boxed{35000 \text{ g O}_2} = 35.0 \text{ kg} \sim 77 \text{ lb}$$

CHEMICAL CALCULATIONS WITH THE GAS LAWS

$$FW_{\text{NaHCO}_3} = 84.007 \text{ g/mol}$$



Given 25.0 g of sodium bicarbonate and sufficient sulfuric acid, what volume of carbon dioxide gas would be produced at 25.0 C and 0.950 atm pressure?

- 1 - Convert 25.0 grams sodium bicarbonate to moles. Use FORMULA WEIGHT.
- 2 - Convert moles sodium bicarbonate to moles carbon dioxide. Use CHEMICAL EQUATION.
- 3 - Convert moles carbon dioxide to volume. Use IDEAL GAS EQUATION.

$$\textcircled{1} 84.007 \text{ g NaHCO}_3 = 1 \text{ mol NaHCO}_3 \quad \textcircled{2} 2 \text{ mol NaHCO}_3 = 2 \text{ mol CO}_2$$

$$25.0 \text{ g NaHCO}_3 \times \frac{1 \text{ mol NaHCO}_3}{84.007 \text{ g NaHCO}_3} \times \frac{2 \text{ mol CO}_2}{2 \text{ mol NaHCO}_3} = 0.2975942481 \text{ mol CO}_2$$

$$\textcircled{3} \begin{array}{l} PV = nRT \\ V = \frac{nRT}{P} \end{array} \quad \begin{array}{l} n = 0.2975942481 \text{ mol CO}_2 \\ R = 0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}} \\ T = 25.0^\circ\text{C} = 298.2 \text{ K} \\ P = 0.950 \text{ atm} \end{array}$$

$$V = \frac{(0.2975942481 \text{ mol CO}_2)(0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}})(298.2 \text{ K})}{(0.950 \text{ atm})} = 7.67 \text{ L of CO}_2 \text{ at } 0.950 \text{ atm, } 25.0^\circ\text{C}$$

What volume would the gas in the last example problem have at STP?

STP: "Standard Temperature and Pressure" (0 C and 1 atm)

We can convert the answer to the previous problem to a volume at STP using the COMBINED GAS LAW.

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$P_1 = 0.950 \text{ atm}$$

$$P_2 = 1 \text{ atm}$$

$$V_1 = 7.67 \text{ L}$$

$$V_2 = ?$$

$$T_1 = 298.2 \text{ K}$$

$$T_2 = 0^\circ \text{C} = 273.2 \text{ K}$$

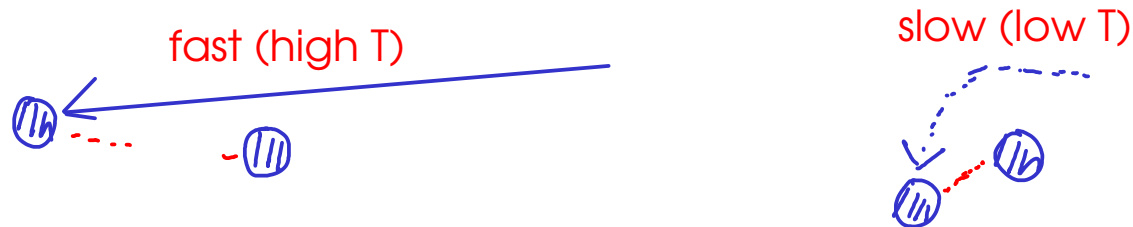
$$\frac{(0.950 \text{ atm})(7.67 \text{ L})}{298.2 \text{ K}} = \frac{(1 \text{ atm}) V_2}{273.2 \text{ K}}$$

$$\boxed{6.67 \text{ L at STP}} = V_2$$

(Alternate solution: Since we'd already calculated moles of gas, plug that and the pressure and temperature from STP into $PV=nRT$...)

REAL GASES

- The empirical gas laws (including the ideal gas equation) do not always apply.
 - The gas laws don't apply in situations where the assumptions made by kinetic theory are not valid.
 - When would it be FALSE that the space between gas molecules is much larger than the molecules themselves?
 - at high pressure, molecules would be much closer together!
 - When would it be FALSE that attractive and repulsive forces would be negligible?
 - at high pressure, attractions and repulsions should be stronger!
 - at low temperature, attractions and repulsions have a more significant affect on the paths of molecules



- The gas laws are highly inaccurate near the point where a gas changes to liquid!
- In general, the lower the pressure and the higher the temperature, the more IDEAL a gas behaves.

van der Waals equation

- an attempt to modify $PV = nRT$ to account for several facts.
 - gas molecules actually have SIZE (they take up space)
 - attractive and repulsive forces

$$PV = nRT \quad] \text{ Ideal gas equation}$$

$$\left(P + \frac{n^2 a}{V^2} \right) (V - nb) = nRT \quad] \text{ van der Waals equation}$$

attempts to account for attractive / repulsive forces

attempts to account for molecular size

* "a" and "b" are experimentally determined parameters that are different for each gas. p 208

He: $a = 0,0346$, $b = 0,0238$ tiny, no special attractive forces

H₂O: $a = 5,537$, $b = 0,03049$ small, but strong attractions between molecules

CH₃CH₂OH: $a = 12,56$ $b = 0,08710$ larger, and strong attractions between molecules

2500 L of chlorine gas at 25.0 C and 1.00 atm are used to make hydrochloric acid. How many kilograms of hydrochloric acid could be produced if all the chlorine reacts?



1 - Convert 2500 L chlorine gas to moles. Use IDEAL GAS EQUATION.

2 - Convert moles chlorine gas to moles HCl. Use CHEMICAL EQUATION

3 - Convert moles HCl to mass. Use FORMULA WEIGHT.

$$\textcircled{1} \begin{array}{l} PV = nRT \\ n = \frac{PV}{RT} \end{array} \quad \left| \quad \begin{array}{l} P = 1.00 \text{ atm} \\ V = 2500 \text{ L} \end{array} \quad \begin{array}{l} R = 0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}} \\ T = 25.0^\circ \text{C} = 298.2 \text{ K} \end{array}$$

$$n_{\text{Cl}_2} = \frac{(1.00 \text{ atm})(2500 \text{ L})}{(0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}})(298.2)} = 102.1646983 \text{ mol Cl}_2$$

$$\textcircled{2} \text{ mol Cl}_2 = 2 \text{ mol HCl} \quad \textcircled{3} \text{ HCl} - \begin{array}{l} \text{H: } 1 \times 1.008 \\ \text{Cl: } 1 \times 35.45 \end{array}$$

②

③

$$102.1646983 \text{ mol Cl}_2 \times \frac{2 \text{ mol HCl}}{\text{mol Cl}_2} \times \frac{36.458 \text{ g HCl}}{\text{mol HCl}} = 7450 \text{ g HCl}$$

$$\text{Kg} = 10^3 \text{ g}$$

$$7450 \text{ g HCl} \times \frac{\text{Kg}}{10^3 \text{ g}} = \boxed{7.45 \text{ Kg HCl}}$$



If 48.90 mL of 0.250 M HCl solution reacts with sodium carbonate to produce 50.0 mL of carbon dioxide gas at 290.2 K, what is the pressure of the carbon dioxide gas?

1 - Convert 48.90 mL of 0.250 M HCl to moles. Use MOLARITY.

2 - Convert moles HCl to moles carbon dioxide. Use CHEMICAL EQUATION.

3 - Convert moles carbon dioxide to pressure. Use IDEAL GAS EQUATION.

$$\textcircled{1} 0.250 \text{ mol HCl} = \text{L}; \text{ mL} = 10^{-3} \text{ L} \quad \textcircled{2} 2 \text{ mol HCl} = \text{mol CO}_2$$

$$48.90 \text{ mL} \times \frac{10^{-3} \text{ L}}{\text{mL}} \times \frac{0.250 \text{ mol HCl}}{\text{L}} \times \frac{\text{mol CO}_2}{2 \text{ mol HCl}} = 0.0061125 \text{ mol CO}_2$$

$$\textcircled{3} \begin{array}{l} PV = nRT \\ p = \frac{nRT}{V} \end{array} \quad \left| \quad \begin{array}{l} n = 0.0061125 \text{ mol CO}_2 \\ R = 0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}} \\ T = 290.2 \text{ K} \end{array} \quad \begin{array}{l} V = 50.0 \text{ mL} = 0.0500 \text{ L} \end{array}$$

$$P = \frac{(0.0061125 \text{ mol CO}_2)(0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}})(290.2 \text{ K})}{0.0500 \text{ L}}$$

$$= \boxed{2.91 \text{ atm}} \text{ of CO}_2 \text{ at } 50.0 \text{ mL, } 290.2 \text{ K}$$

- thermodynamics: the study of energy transfer

Conservation of energy: Energy may change form, but the overall amount of energy remains constant. "first law of thermodynamics"

- ... but what IS energy?

- energy is the ability to do "work"

↑
motion of matter

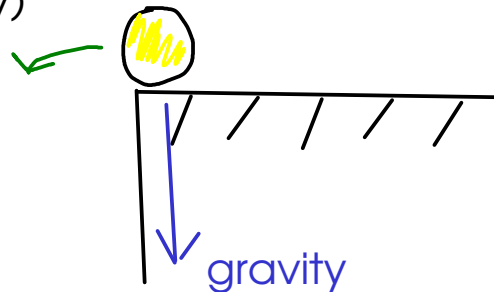
Kinds of energy?

- Kinetic energy: energy of matter in motion $E_K = \frac{1}{2} m v^2$

mass

velocity

- Potential energy: energy of matter that is being acted on by a field of force (like gravity)



When the ball falls, its potential energy is converted to kinetic!

- What sort of energy concerns chemists? Energy that is absorbed or released during chemical reactions.

- Energy can be stored in chemicals ... molecules and atoms.

INTERNAL ENERGY: "U"



related to the kinetic and potential energy of atoms, molecules, and their component parts.

- We measure energy transfer ... which is called HEAT. (HEAT is the flow of energy from an area of higher temperature to an area of lower temperature)

Q: heat

SYSTEM: the object or material under study

SURROUNDINGS: everything else

Type of process	Energy is ...	Sign of Q	Temp of SURROUNDINGS ...
ENDOTHERMIC	transferred from SURROUNDINGS to SYSTEM	+	decreases
EXOTHERMIC	transferred from SYSTEM to SURROUNDINGS	-	increases