$$49 = \frac{X}{(0.100-x)(0.100-x)}$$

$$49 = \frac{X}{(0.100-x)^2}$$

$$49(0.100-x)^2 = X$$

$$\downarrow (a-b)^2 = a^2 - 2ab + b^2$$

$$49(0.0100 - 0.200x + x^2) = X$$

$$0.49 - 9.8x + 49x^2 = X$$

$$0.49 - 10.8x + 49x^2 = 0$$

$$c = 0.49 \quad b = -10.8 \quad a = 49$$

$$X = \frac{10.8 \pm \sqrt{(-10.8)^2 - 4(49)(0.49)}}{2(49)} = \frac{10.8 \pm \sqrt{20.6}}{98}$$

$$x = 0.157 \text{ or } 0.0639 \text{ ... but only one of these answers works chemically!}$$

The QUADRATIC EQUATION:

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Each quadratic has two solutions (see the +/- part of the equation), but onlu one of them will be the correct chemical solution.

If we look at the value 0.157 for x, we find that it gives impossible (negative) values for the equilibrium concentrations of both chlorine gas and phosphorus trichloride. Therefore, the second value (0.0639) must be the correct value for x ...

Species	[Initial]	Δ	[Equilibrium]
PCl_5	0	$+X$	X
PCl_3	$\dfrac{0.400 \text{ mol}}{4.00 L} = 0.100$	$-X$	$0.100 - X$
Cl_2	$\dfrac{0.400 \text{ mol}}{4.00 L} = 0.100$	$-X$	$0.100 - X$

$X = 0.0639$

To find the equilibrium concentrations, plug the value of x into the (Equilibrium) column in the chart...
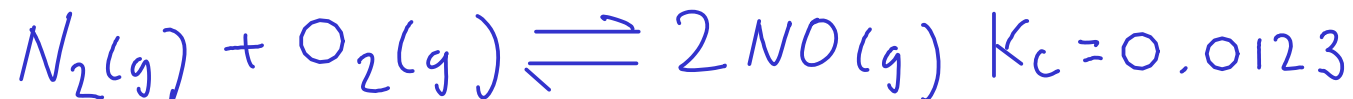
$[PCl_5] = X = 0.064 \, M \, PCl_5$

$[PCl_3] = 0.100 - X = 0.036 \, M \, PCl_3$

$[Cl_2] = 0.100 - X = 0.036 \, M \, Cl_2$

Since Kc = 49, we expect that the products will be favored at equilibrium, so these concentrations look reasonable.

An 8.00 L reaction vessel at 3900C is charged with 0.850 mol of nitrogen and oxygen gases. Find the concentration of all species at equilibrium.

$$N_2(g) + O_2(g) \rightleftharpoons 2NO(g) \quad K_c = 0.0123$$

$$K_c = 0.0123 = \frac{[NO]^2}{[N_2][O_2]}$$

We need to express these in terms of a single variable to solve ...

Species	[Initial]	Δ	[Equilibrium]
N_2	$\frac{0.850\ mol}{8.00\ L} = 0.10625$	$-X$	$0.10625 - X$
O_2	$\frac{0.850\ mol}{8.00\ L} = 0.10625$	$-X$	$0.10625 - X$
NO	0	$+2x$	$2x$

Let "x" equal the change in nitrogen gas concentration...

Substitute and solve...

$$0.0123 = \frac{[NO]^2}{[N_2][O_2]}$$

$$0.0123 = \frac{(2x)^2}{(0.10625 - x)(0.10625 - x)}$$

$$\frac{(2x)^2}{(0.10625-x)(0.10625-x)} = 0.0123$$

$$\frac{(2x)^2}{(0.10625-x)^2} = 0.0123$$

this could be solved using the quadratic equation, but an alternative is to take the square root of both sides, since the entire left hand side of the equation is a squared term ...

$$\sqrt{\frac{(2x)^2}{(0.10625-x)^2}} = \sqrt{0.0123}$$

$$\frac{2x}{0.10625-x} = 0.1109053651$$

$$\frac{2}{0.1109053651} x = 0.10625-x$$

$$18.03339269\,x = 0.10625-x$$

$$19.03339269\,x = 0.10625$$

$$x = 0.0055822943$$

Now, find concentrations...

Species	[Equilibrium]
N_2	$0.10625-x$
O_2	$0.10625-x$
NO	$2x$

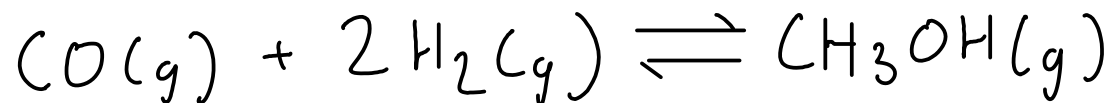$$[N_2] = 0.101\ M\ N_2$$
$$[O_2] = 0.101\ M\ O_2$$
$$[NO] = 0.0112\ M\ NO$$

As expected, the concentration of NO is much smaller than the reactant concentrations...

- Pressure can affect a GAS-PHASE equilibrium ... sometimes. How?

$$CO(g) + 2H_2(g) \rightleftharpoons CH_3OH(g)$$

... how might pressure affect this equilibrium?

- If the change in pressure CHANGES CONCENTRATIONS, then this equilibrium would be disturbed and Le Chateleir's Principle would apply.

- Adding an INERT GAS would change pressure, but would it change concentration of the gases? NO - so addition of argon would have no effect on the equilibrium!
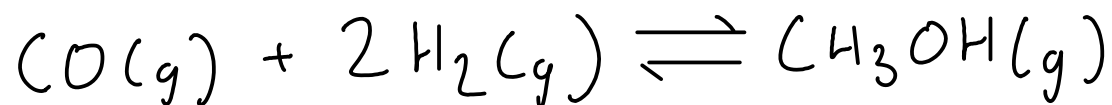
- What about COMPRESSION?

CO V		←P
H₂		
CH₃OH		

½V		←2P
CO		
H₂		
CH₃OH		
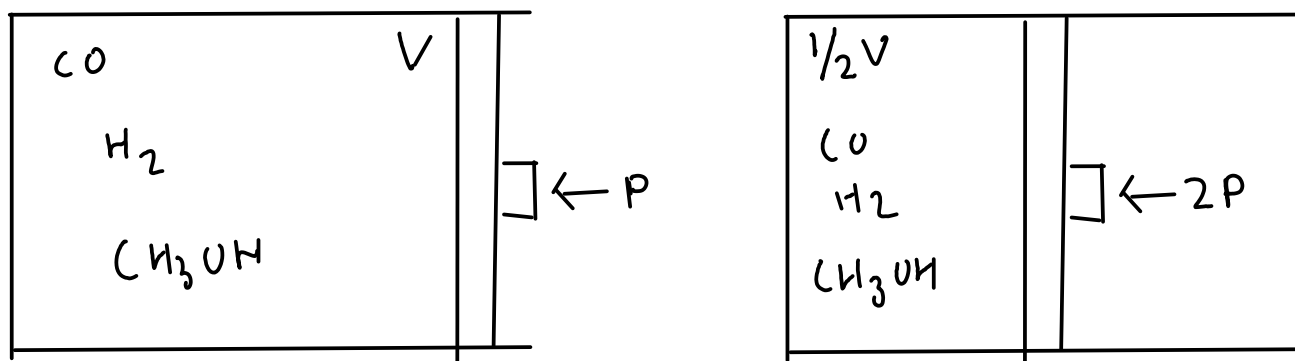
... compression increases pressure by DECREASING total volume.
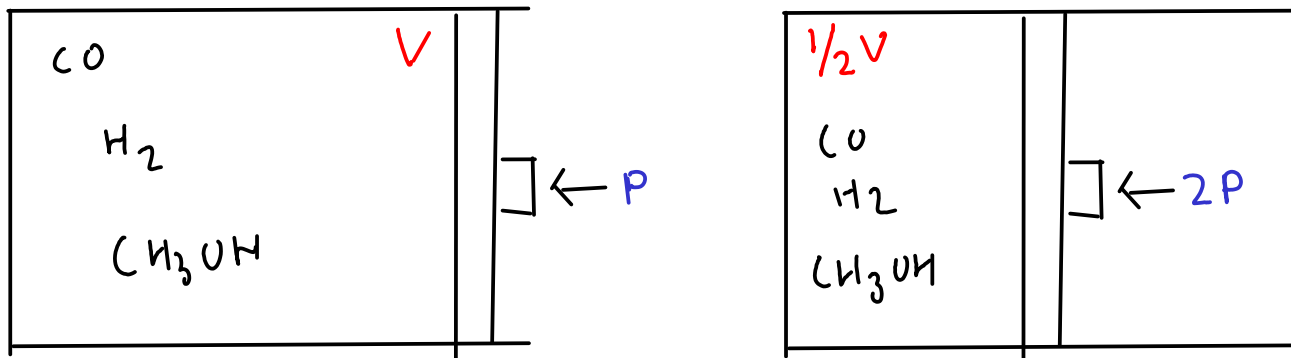
... but this volume change affects ALL concentrations the same way. In this example, each concentration is DOUBLED.

$$CO(g) + 2H_2(g) \rightleftharpoons CH_3OH(g)$$

$$K_c = \frac{[CH_3OH]}{[CO][H_2]^2} \qquad \frac{(1)}{(1)(1)^2} = 1$$

For simplicity, let's assume Kc = 1, and all concs = 1M

Doubling concentrations gives Q= $\dfrac{2}{(2)(2)^2} = \dfrac{1}{4}$

$Q < K_c$, so equilibrium shifts to the RIGHT, forming more methanol at the expense of hydrogen and carbon monoxide.

In general, compressing an equilibrium reaction in the gas phase will cause the equilibrium to shift towards the side with fewer moles of gas. This causes the pressure to decrease.

In general, decompressing an equilibrium reaction in the gas phase will cause the equilibrium to shift towards the side with more moles of gas. This causes the pressure to increase.

HOWEVER, this can only be true IF there's a side of the reaction with more moles of gas than the other. If both sides of the reaction have the SAME number of moles of gas, then a pressure change will NOT affect the equilibrium.

Example: $N_2(g) + O_2(g) \rightleftharpoons 2\,NO(g)$
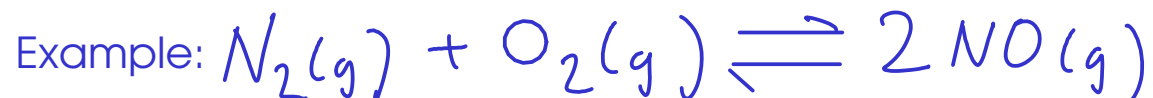
... would not respond to a pressure change.

FACTORS THAT MAY AFFECT EQUILBRIUM

① TEMPERATURE (effect depends on whether reaction is endothermic or exothermic)

   - Changes rate of reaction, too!
   ... changes Kc

② PRESSURE - only for gas-phase reactions which have different numbers of moles of gas on each side of the equilbrium. Otherwise, no effect.

   ... no change of Kc

③ CATALYSTS - do NOT affect equilibrium, but make the equilbrium state occur more quickly.

A B*

C+D

A+B
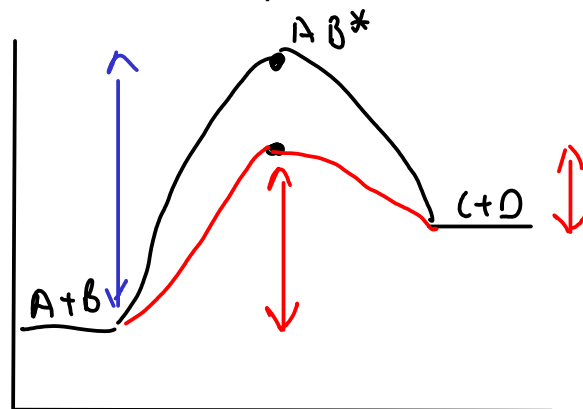
The catalyst raises BOTH forward and reverse rates, so it doesn't affect the composition of the equilibrium mixture!

④ CONCENTRATION - Le Chateleir's Principle applies for changing concentrations. An equilibrium will shift to counteract a change in concentration of reactant or product.

   ... doesn't change Kc.

ACID/BASE EQUILIBRIUM

- Several scientific theories exist that define acid-base chemistry. We will discuss THREE of these theories.

- These theories differ in the way that acids, bases, and their associated reactions are defined.

- Typically, the newer theories include MORE chemicals under the umbrella of "acid-base chemistry"!

THREE ACID-BASE THEORIES

① Arrhenius theory

② Bronsted-Lowry theory

③ Lewis theory

ARRHENIUS THEORY

- The oldest model of acid-base chemistry!

- Only applicable to systems where WATER is the solvent!

ACIDS are substances that ionize in water to increase the concentration of HYDRONIUM ION

$$HA + H_2O \rightleftharpoons H_3O^+ + A^-$$

Hydronium ion

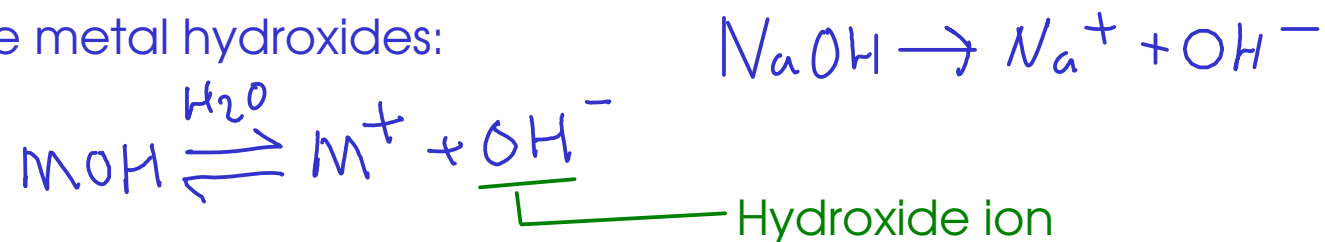or, for simplicity: $HA \underset{}{\overset{H_2O}{\rightleftharpoons}} H^+ + A^-$

"Hydrogen ion" - doesn't really exist as a free ion in water, but a convenient simplification!

ARRHENIUS THEORY

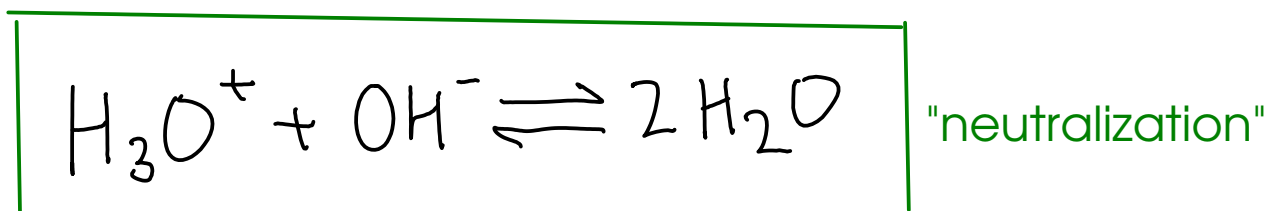BASES are substances that ionize in water to increase the concentration of HYDROXIDE ION

For soluble metal hydroxides:

$$NaOH \rightarrow Na^+ + OH^-$$

$$MOH \underset{H_2O}{\rightleftharpoons} M^+ + OH^-$$

— Hydroxide ion

For other Arrhenius bases:

$$B + H_2O \rightleftharpoons BH^+ + OH^- \qquad ex: NH_3$$

An Arrhenius acid base reaction can be represented by:

$$H_3O^+ + OH^- \rightleftharpoons 2H_2O$$

"neutralization"

or, using hydrogen ion instead of hydronium

$$H^+ + OH^- \rightleftharpoons H_2O$$