

136- Temperature:

- a measure of the average kinetic energy of the molecules of the gas

$$E_k = \frac{1}{2} m v^2$$

velocity
mass

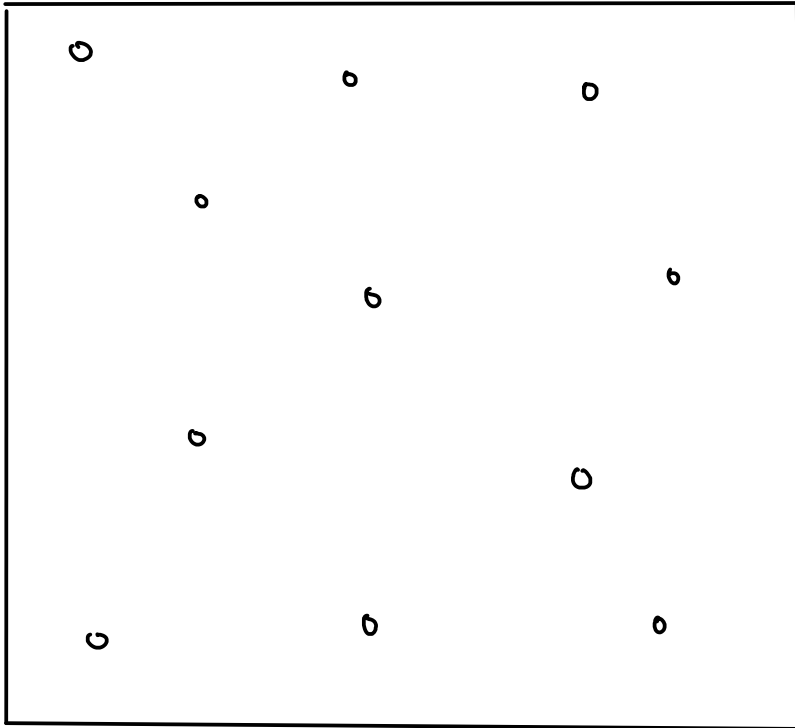
- The faster the gas molecules move, the higher the temperature!
- The temperature scales used when working with gases are ABSOLUTE scales.
 - ABSOLUTE: scales which have no values less than zero.
 - KELVIN: metric absolute temperature scale.

Quick comparison of temperature scales!

$$K = 273.15 + ^\circ C$$

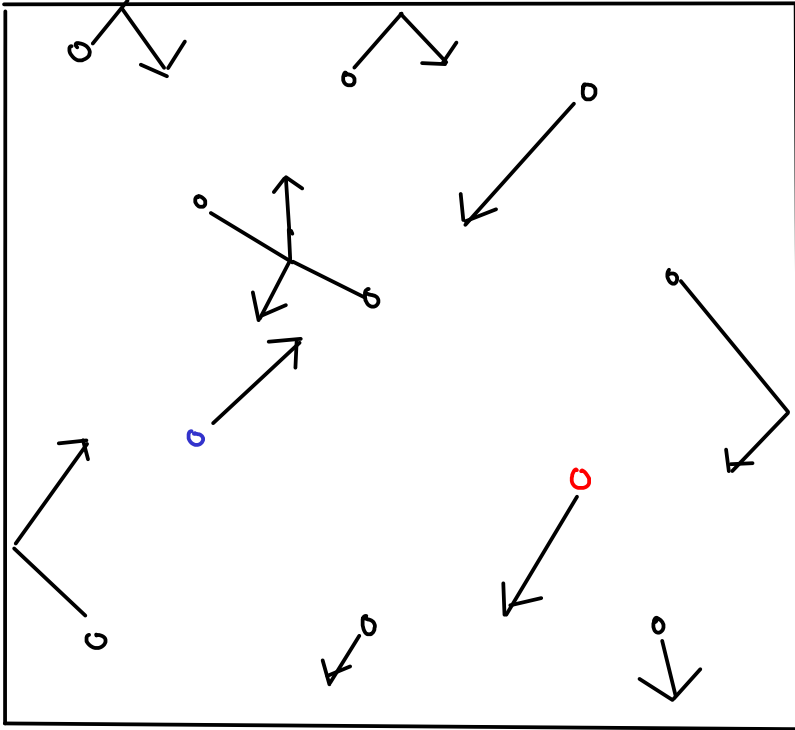
212	100	373	Water boils
77	25	298	Room temperature
32	0	273	Water freezes
-460	-273	0	Absolute zero!
$^{\circ}F$	$^{\circ}C$	K	

THE KINETIC PICTURE OF GASES



LOW DENSITY!

① Gas molecules are small compared to the space between the gas molecules!



- ② Gas molecules are constantly in motion. They move in straight lines in random directions and with various speeds.
- ③ Attractive and repulsive forces between gas molecules are so small that they can be neglected except in a collision.
 - Each gas molecule behaves independently of the others.
- ④ Collisions between gas molecules and each other or the walls are ELASTIC.

⑤ The average kinetic energy of gas molecules is proportional to the absolute temperature.

How does this picture explain the properties of gases?

- Gases expanding to fill their container? Agrees with kinetic picture, since gas molecules are independent
- Thermal expansion of gas at constant pressure? Agrees, because the container has to EXPAND to keep the pressure (from collisions) constant when the gas molecules move faster.
- Pressure increases with temperature at constant volume: Agrees, because the number and force of collisions increases with molecular speed.

GAS LAWS

- were derived by experiment long before kinetic theory, but agree with the kinetic picture!

Boyle's Law:

$$PV = \text{constant} \quad \left. \vphantom{PV = \text{constant}} \right] \text{ True at constant temperature}$$

$$P_1 V_1 = \text{constant}$$

$$P_2 V_2 = \text{constant}$$

$$\left. \vphantom{P_1 V_1 = \text{constant}} \right] \rightarrow \boxed{P_1 V_1 = P_2 V_2} \quad \text{True at constant temperature}$$

Charles's Law:

$$\frac{V}{T} = \text{constant} \quad \left. \vphantom{\frac{V}{T} = \text{constant}} \right] \text{ True at constant pressure, and using ABSOLUTE temperature}$$

$$\left. \vphantom{\frac{V}{T} = \text{constant}} \right] \rightarrow \boxed{\frac{V_1}{T_1} = \frac{V_2}{T_2}} \quad \text{True at constant pressure, and using ABSOLUTE temperature}$$

140 Combined gas law:

$$\frac{PV}{T} = \text{constant}$$

Must use ABSOLUTE temperature units!

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

Must use ABSOLUTE temperature units!

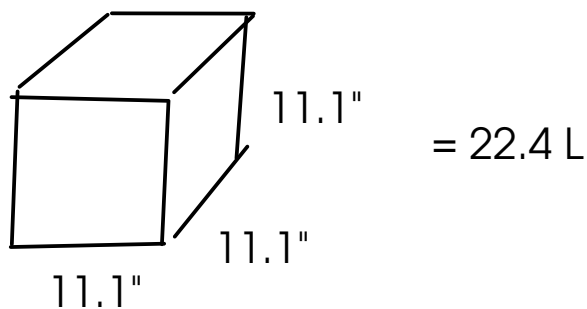
↑ amount (moles) of gas must be constant!

Avogadro's law:

- a mole of any gas at the same conditions has the same volume.

1 mol gas molecules @ 0°C and 1 atm
volume = 22.4 L

"STP"
Standard
Temperature
and
Pressure



Ideal gas law:

$$\frac{PV}{T} = \text{constant}$$

... but this constant actually depends on the amount of gas!

$$= n \times "R"$$

The ideal gas constant,

$$0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}}$$

... combining these together ...

$$\frac{PV}{T} = nR$$



$$PV = nRT$$

P = pressure atm

V = volume L

T = ABSOLUTE temperature K

R = ideal gas constant

n = number of moles of gas molecules

A balloon is taken from a room where the temperature is 27.0 C to a freezer where the temperature is -5.0 C. If the balloon has a volume of 3.5 L in the 27.0 C room, what is the volume of the balloon in the freezer. Assume pressure is constant.

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \quad \text{Since } P_1 = P_2 \text{ (constant } P), \quad \frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$V_1 = 3.5 \text{ L}$$

$$V_2 = ? \text{ L}$$

$$T_1 = 27.0^\circ\text{C} = 300.2 \text{ K} \quad \left\{ \quad T_2 = -5.0^\circ\text{C} = 268.2 \text{ K} \right.$$

$$\frac{3.5 \text{ L}}{300.2 \text{ K}} = \frac{V_2}{268.2 \text{ K}} ; \quad V_2 = \boxed{3.1 \text{ L in freezer}}$$

2.25 L of nitrogen gas is trapped in a piston at 25.0 C and 1.00 atm pressure. If the piston is pushed in so that the gas's volume is 1.00 L while the temperature increases to 31.0 C, what is the pressure of the gas in the piston?

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \quad \begin{array}{l} P_1 = 1.00 \text{ atm} \\ V_1 = 2.25 \text{ L} \\ T_1 = 25.0^\circ\text{C} = 298.2 \text{ K} \end{array} \quad \begin{array}{l} P_2 = ? \\ V_2 = 1.00 \text{ L} \\ T_2 = 31.0^\circ\text{C} = 304.2 \text{ K} \end{array}$$

$$\frac{(1.00 \text{ atm})(2.25 \text{ L})}{(298.2 \text{ K})} = \frac{P_2 (1.00 \text{ L})}{(304.2 \text{ K})} ; \quad P_2 = \boxed{2.30 \text{ atm}}$$

Calculate the mass of ^{*}22650 L of oxygen gas at 25.0 C and 1.18 atm pressure.



*Volume of a 10'x10'x8' room

Use the ideal gas equation to find MOLES of gas, then convert to MASS using the formula weight.

$$PV = nRT$$

$$\frac{PV}{RT} = n$$

$$P = 1.18 \text{ atm}$$

$$R = 0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}}$$

$$V = 22650 \text{ L}$$

$$T = 25.0^\circ\text{C} = 298.2 \text{ K}$$

$$\frac{(1.18 \text{ atm})(22650 \text{ L})}{(0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}})(298.2 \text{ K})} = n_{\text{O}_2} = 1092.222357 \text{ mol O}_2$$

Now, convert moles oxygen gas to mass oxygen gas using the formula weight...

$$1092.222357 \text{ mol O}_2 \times \frac{32.00 \text{ g O}_2}{\text{mol O}_2} =$$

$$35000 \text{ g O}_2$$

$$35.0 \text{ kg} \\ \sim 77 \text{ lb}$$