

## Measurements

Measurements are COMPARISONS of properties against accepted standards, called units.

A properly-reported measurement has TWO PARTS:  
(1) a measured NUMBER  
(2) a UNIT

### English/US Units:

1 foot = 12 inches    1 yard = 3 feet    1 mile = 1760 yards

5280 feet = 1 mile

So what's the problem?

The English system is messy because it consists of units for the same kinds of things that were developed independently of each other - so we have to memorize a bunch of essentially random numbers just to use the system.

Add to that - each different kind of thing we measure has completely different numbers relating the units ...

English units are nonstandard and difficult to use. Solution?

## THE METRIC SYSTEM

All metric units are made up of COMBINATIONS of BASE UNITS!

Metric Base Units:

Length	meter	m
Mass	*kilogram	kg
Temperature	Kelvin	K
Time	second	s

\*we usually treat the gram as if it's the base unit for mass!

Comparing to the English system:

- One meter is approximately 3.3 feet.
- One kilogram is approximately 2.2 pounds.

What about SIZE?

Metric units may be made larger or smaller by adding PREFIXES.

Metric Prefixes:

mega-	$10^6$	M
kilo-	$10^3$	k
centi-	$10^{-2}$	c
milli-	$10^{-3}$	m
micro-	$10^{-6}$	$\mu$

Bigger units

Memorize  
these  
prefixes!

smaller units

Applying prefixes

$$1 \text{ ___ m} = \text{ ___ m}$$

$$1 \text{ mm} = 10^{-3} \text{ m} \left( \frac{1}{1000} \text{ m} \right)$$

$$1 \text{ km} = 10^3 \text{ m} \left( 1000 \text{ m} \right)$$

## Scaling units with metric prefixes ... examples

The distance between here and Columbia, SC is about 107,000 meters.  
What metric unit would be best suited for a distance like this?

$$K = 10^3 \text{ (1000)}$$

$$km = 1000 \text{ m}$$

$$107 \text{ km}$$

By "best suited", we mean a metric unit that would represent the number without many beginning or end zeros. These kinds of numbers are easier for us to remember!

A piece of chalk is 0.080 meters long. What metric unit would be best suited for this length?

$$C = 10^{-2} \text{ (1/100)}$$

$$cm = \frac{1}{100} \text{ m}$$

$$8 \text{ cm}$$

## Derived Units

- are units that are made up of combinations of metric base units with each other and/or with prefixes

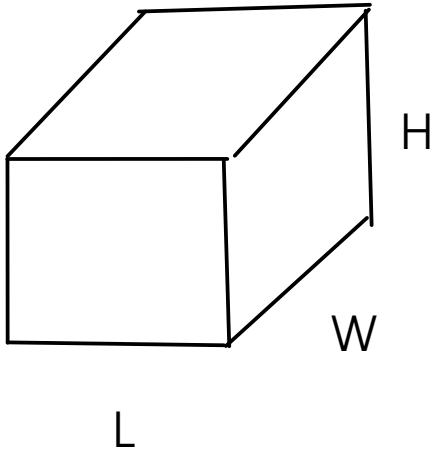
Example: *speed*       $\frac{\text{miles}}{\text{hr}}$  ,  $\frac{\text{Km}}{\text{hr}}$        $\left( \frac{\text{length}}{\text{time}} \right)$  ,  $\frac{\text{m}}{\text{s}}$

Two derived units are particularly important in introductory chemistry:

1) VOLUME

2) DENSITY

## VOLUME



$$\text{VOLUME} = L \times W \times H$$

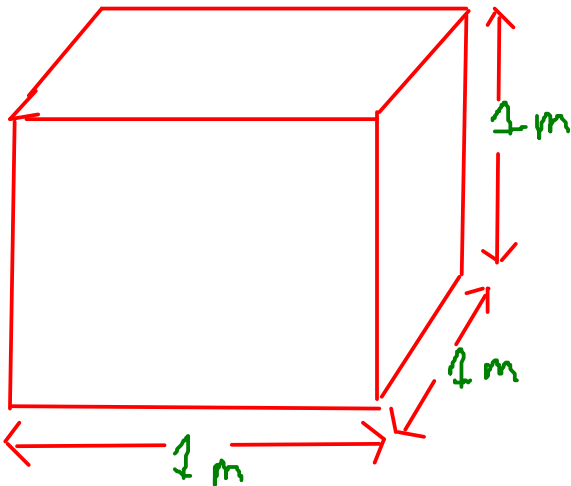
What are the units of volume in the metric system?

$L = \text{LENGTH.} = \text{meter}$

$W = \text{WIDTH.} = \text{meter}$

$H = \text{HEIGHT.} = \text{meter}$

$$\begin{aligned} \text{VOLUME UNIT} &= m \times m \times m \\ &= m^3 \text{ "cubic meters"} \end{aligned}$$



Practical problem: The cubic meter is a very LARGE volume unit for laboratory-scale work.

Solution? We need to scale this unit down by using metric prefixes!

## Practical issues for volume units

- Cubic meters are too large! A meter is very similar in length to a yard, so a cubic meter is a cube that is approximately a yard long on each side!

A smaller unit For volume?

Cubic decimeters!

$\text{dm}^3$

(decimeter =  $\frac{1}{10}$  meter)

Cubic decimeters are given the name "liters", abbreviation "L"

In the lab, we typically need an even smaller unit than the liter, so we use milliliters (mL)

"cc"  
cubic centimeter  
=  
milliliter

$$1 \text{ mL} = 10^{-3} \text{ L}$$

-or-

$$1000 \text{ mL} = 1 \text{ L}$$

## DENSITY

- Density is a measure of the concentration of matter; of how much matter is present in a given space
- Density is defined as the MASS per unit VOLUME, or ...

$$\text{Density} = \frac{\text{mass}}{\text{Volume}}$$

What are the metric units of DENSITY?

mass: kilogram (kg)

volume: cubic meters (m<sup>3</sup>)

So, density unit =  $\frac{\text{kg}}{\text{m}^3}$

These units aren't routinely used in the lab. They're too large (like the volume unit itself).

So we just use our lab units!

Note: Typical lab balances can measure up to several hundred grams (in other words, less than a kilogram)



In the lab, we typically measure masses as grams and volumes as milliliters, so the density unit we will use most often is:

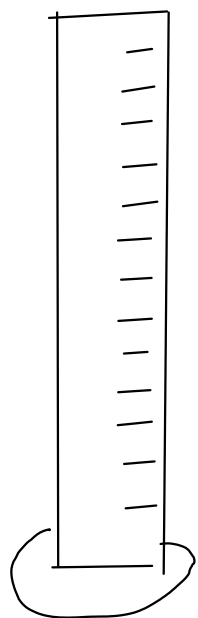
$$\frac{\text{g}}{\text{mL}} \quad \text{Same as} \quad \frac{\text{g}}{\text{cm}^3}$$

A useful density to remember:

WATER at room temp: Density =  $1 \frac{\text{g}}{\text{mL}}$

## Measuring density

... of a liquid



1) Measure mass of empty cylinder

$$\text{mass} = 97.35 \text{ g}$$



2) Fill cylinder and measure volume of liquid

$$\text{volume} = 25.3 \text{ mL}$$

3) Measure mass of filled cylinder

$$\text{mass} = 130.55 \text{ g}$$

4) Subtract to find mass of liquid

$$\begin{array}{r} 130.55 \text{ g} \\ - 97.35 \text{ g} \\ \hline 33.20 \text{ g} \end{array}$$

5) Density = mass liquid / volume liquid

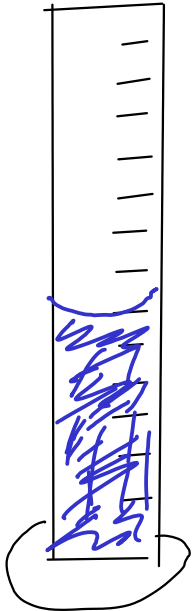
$$\begin{aligned} \text{Density} &= \frac{33.20 \text{ g}}{25.3 \text{ mL}} \\ &= 1.31 \text{ g/mL} \end{aligned}$$

...of an object



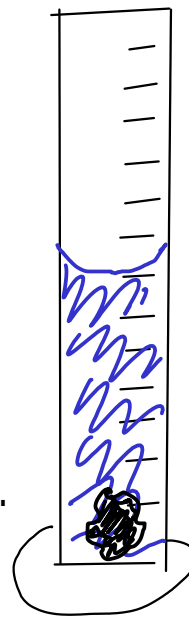
1) Measure mass  
of object

$$\text{mass} = 9.78 \text{ g}$$



2) Partially fill cylinder  
with liquid, record volume.

$$\text{volume} = 25.0 \text{ mL}$$



3) Put object into cylinder, record new  
volume

$$\text{volume} = 26.6 \text{ mL}$$

4) Subtract to find volume of object

$$\begin{array}{r} 26.6 \text{ mL} \\ - 25.0 \text{ mL} \\ \hline 1.6 \text{ mL} \end{array}$$

5) Density = mass object / volume object

$$\text{Density} = \frac{9.78 \text{ g}}{1.6 \text{ mL}}$$

$$= 6.1 \text{ g/mL}$$

## Converting from one unit to another

We will use the method of dimensional analysis, sometimes called the factor-label method.... or, the "drag and drop" method!

Dimensional analysis uses conversion factors to change between one unit and another

What's a conversion factor? A simple equality.

Example

$$12 \text{ in} = 1 \text{ ft}$$

## Conversion factors in metric

In the metric system, conversion factors between units may always be made from the metric prefixes!

For example, "kilo-" means  $10^3$

$$k = 10^3$$

so

$$kg = 10^3 g$$

$$km = 10^3 m$$

$$kL = 10^3 L$$

$$ks = 10^3 s$$

Just apply the prefix to the base unit!

How do we actually USE a conversion factor?

Convert 15.75 m to cm

$$15.75 \cancel{\text{m}} \times \frac{\text{cm}}{10^{-2} \cancel{\text{m}}} = 1575 \text{ cm}$$

$\text{cm} = 10^{-2} \text{ m}$

DRAG  
AND  
DROP!

Put what you want to cancel on  
the bottom, then ...

... put what it equals on the top!

Convert 0.01893 kg to g

$$0.01893 \cancel{\text{kg}} \times \frac{10^3 \text{ g}}{\cancel{\text{kg}}} = 18.93 \text{ g}$$

$\text{kg} = 10^3 \text{ g}$